Variational Methods and Structural Optimization

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1. The displacement field for a deep isotropic beam is given by

$$u(x, z, t) = u(x, t)$$

$$w(x, z, t) = z\psi(x, t)$$

where u(x,t) is the axial displacement and w(x,t) is the transverse displacement. $\psi(x,t)$ is the degree of freedom that represents the poisson's effect. The constitutive relations for the deep rod is given by

$$\left\{ \begin{array}{c} \sigma_{xx} \\ \sigma_{zz} \\ \tau_{xz} \end{array} \right\} = (E)/(1-\nu^2) \left[\begin{array}{ccc} 1 & \nu & 0 \\ \nu & 1 & 0 \\ 1 & 1 & \frac{1-\nu}{2} \end{array} \right] \left\{ \begin{array}{c} \epsilon_{xx} \\ \epsilon_{zz} \\ \gamma_{xz} \end{array} \right\}.$$

Derive equation of motion(using Hamilton's principle) for this deep rod and its associated force boundary conditions.