## Exercise Problems for Module 5

- [P5.1] In the development of the angular velocity vector, we defined a space-fixed and a body-fixed angular velocity vector. Can you think of any example where the body-fixed angular velocity would be natural to use?
- [P5.2] Derive the *space-fixed* and *body-fixed* angular velocity matrices and vectors for a rotation matrix obtained from a X Y Z Euler angle rotations of a rigid body.
- [P5.3] Given a rotation matrix  ${}^A_B[R]$  in terms of axis and angle, i.e., as  $[R(\hat{\mathbf{k}},\phi)]$ , obtain the *space-fixed* and *body-fixed* angular velocity vector components in terms of  $\hat{\mathbf{k}}$  and  $\phi$  and their derivatives with respect to time.
- [P5.4] Derive the velocity propagation equations for a serial manipulator with two consecutive links connected by prismatic (P) joints.
- [P5.5] Using MAPLE or otherwise derive the expressions for the elements of the Jacobian matrix of a PUMA 560 robot described in Module 2.
- [P5.6] Obtain the Jacobian matrix for the planar 3R manipulator in  $\{Tool\}$ . What is the general rule for transforming a  $6 \times n$  Jacobian matrix between two coordinate systems?
- [P5.7] Prove that [g] is positive definite. Obtain the eigenvectors for [g] corresponding to the eigenvalues  $\lambda_1$  and  $\lambda_2$ . What do the eigenvectors mean?
- [P5.8] For the five-bar mechanism shown in problems for Module 4 see Problems-4.pdf obtain [K], and  $[K^*]$ . Describe geometrically, similar to the planar four-bar example, what happens when  $\det([K^*]) = 0$ .
- [P5.9] Write a program to search and obtain another configuration of the three- degree-of-freedom manipulator where linear velocity ellipsoid degenerates to an ellipse.
- [P5.10] Write a program to search and obtain another configuration where the three- degree-of-freedom manipulator gains a degree of freedom.
- [P5.11] Obtain the force transformation matrix for the three- degree-of-freedom parallel manipulator discussed in Example 5.3.

[P5.12] For a six- degree-of-freedom serial manipulator in a singular configuration, it is known that all the joint axes intersect a line perpendicularly. For the PUMA 560 discussed in Module 2, verify this fact and obtain the equation of this line.